### Density functional calculations for small iron clusters with substitutional phosphorus

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### Abstract

The embrittlement is known to be caused by phosphorus (P) segregation at grain boundaries (BGs) in iron (Fe) alloy. Effects of P substitutions on binding energies and electronic structures of octahedral Fe cluster are investigated using density functional calculations in order to understand nature of bonding between P and Fe atoms at GBs. The binding energies increase in  $Fe_3P_3$  and Fe-rich clusters while they decrease in P-rich clusters. The changes of binding energies are closely connected to the charge transfer from Fe to P atoms. The charge transfer leads to both stronger and weaker bonds in mixed Fe-P clusters. The weaker bonds due to less charge occur embrittlement. The calculations indicate that the binding energies and chemical bondings are affected by atomic configurations of P atoms in Fe-P clusters.



## Background and Objective

### Background

- O The embrittlement in Fe alloy under thermal or irradiation environment is the serious issue for structural materials in fusion and fission reactors.
- $\bigcirc$  The embrittlement is closely connected to the segregation of impurities at GB.
- $\bigcirc$  The impurity segregation at the GBs is promoted by irradiation.
- P atom is one of the impurities in Fe alloy, and is considered to be one of the embrittling elements.
- The P segregation is believed to weaken cohesion at Fe GBs.

### Objective

- Understanding on effects of P atoms segregated at Fe GBs.
  - ★ We perform ab initio calculations on the changes of binding energies and structural and electronic properties of Fe<sub>6</sub> cluster induced by P substitutions.



### Summary

Our DFT calculations predict effects of P substitutions for equilibrium geometry, binding energy and electron properties of Fe<sub>6</sub> clusters. Based on the calculations the effects of chemical bonding on GB embrittlement is considered. The changes of binding energies in Fe-P clusters are found to be closely connected to the charge transfer from Fe to P atoms. As shown by calculations of Fe<sub>3</sub>P<sub>3</sub> and Fe-rich clusters, a small number of P atoms stabilize the Fe GBs as well as lead to the strengthening of Fe-P bonds and the weakening of Fe-Fe bonds. The weaker bondings due to less charge occur embrittlement while the stronger bondings due to more charge stabilize GBs. In contrast to this, a large number of P atoms, which is adjacent to each other, induce unstable GBs due to weaker Fe-P and P-P bondings, and the weaker bondings occur embrittlement.

Atomic configurations of GBs with P-enrichment induced by irradiation are complex. As shown by our calculations, the cause of P embrittlement is affected by the atomic configurations of P atoms in GB. Thus, the effects of more than one P segregation should not be neglected.



### **Computational details**

- Theory: DFT-(U)B3LYP/LanL2DZ
  - Code: Gaussian03
- Clusters:  $Fe_{6-x}P_x$  ( $0 \le x \le 6$ )
- Binding energies  $(E_b)$ : The binding energies per atom of clusters are calculated with respect to the Fe atom with M = 5 and P atom with M = 4. M means spin multiplicities.
- Natural population analysis: electron configuration, natural population and natural atomic orbital (NAO) bond order are calculated.





# Binding energies, bond lengths, and NAO bond orders of Fe-P clusters

				R <sub>e</sub>			NAO bond order		
System	Symm.	Μ	Eb	Fe-Fe	Fe-P	P-P	Fe-Fe	Fe-P	Р-Р
Fe <sub>6</sub>	D <sub>4h</sub>	21	1.85	2.43, 2.45			0.36		
Fe₅P	C <sub>4v</sub>	16	2.00	2.42, 2.53	2.49		0.28, 0.34, 0.38	0.39, 0.40	
Fe <sub>4</sub> P <sub>2</sub>	D <sub>4h</sub>	13	2.11	2.42	2.50		0.22	0.37, 0.40	
	<b>C</b> <sub>2v</sub>	13	2.19	2.56, 2.74	2.38, 2.40	3.72	0.23, 0.28	0.49, 0.44	0.07
Fe <sub>3</sub> P <sub>3</sub>	C <sub>3v</sub>	12	1.97	2.46	2.60	2.50	0.41	0.29	0.54
	<b>C</b> <sub>2v</sub>	10	2.06	2.46, 2.67	2.34, 2.36, 2.42	3.47	0.14, 0.12	0.46, 0.48, 0.42	0.10
Fe <sub>2</sub> P <sub>4</sub>	D <sub>4h</sub>	7	1.83		2.37	2.82		0.37, 0.38	0.37
	<b>C</b> <sub>2v</sub>	7	1.86	2.37	2.37, 2.48	2.23, 3.07	0.25	0.48, 0.34	0.89, 0.21
FeP₅	C <sub>4v</sub>	4	1.58		2.48	2.57, 2.76		0.33, 0.35	0.49, 0.35
P <sub>6</sub>	D <sub>4h</sub>	3	1.09			2.61, 2.82			0.45, 0.26
$\mathbf{Y}(\mathbf{x})$	E <sub>b</sub> : eV/atom, R <sub>e</sub> : Å							<b>∴Å</b>	

# Natural electron configurations and natural populations of Fe-P clusters (1)

System	Symm.	Atom	Natural electron configuration	Natural population
Fe <sub>6</sub>	D <sub>4h</sub>	Fe(1-4)	[core]4s <sup>1.09</sup> 3d <sup>6.81</sup> 4p <sup>0.08</sup> 5s <sup>0.01</sup> 4d <sup>0.02</sup>	0.00
		Fe(5, 6)	[core]4s <sup>1.09</sup> 3d <sup>6.80</sup> 4p <sup>0.08</sup> 5s <sup>0.01</sup> 4d <sup>0.02</sup>	0.01
Fe₅P	<b>C</b> <sub>4v</sub>	Fe(1, 3)	[core]4s <sup>0.86</sup> 3d <sup>6.82</sup> 4p <sup>0.06</sup> 4d <sup>0.01</sup> 5s <sup>0.01</sup> 4d <sup>0.01</sup>	0.24
		Fe(2, 4)	[core]4s <sup>0.74</sup> 3d <sup>6.93</sup> 4p <sup>0.06</sup> 4d <sup>0.01</sup>	0.25
		P(5)	[core]3s <sup>1.90</sup> 3p <sup>4.01</sup>	-0.91
		Fe(6)	[core]4s <sup>1.18</sup> 3d <sup>6.76</sup> 4p <sup>0.10</sup> 5s <sup>0.02</sup> 4d <sup>0.01</sup>	-0.06
Fe <sub>4</sub> P <sub>2</sub>	D <sub>4h</sub>	Fe(1, 3)	[core]4s <sup>0.58</sup> 3d <sup>6.84</sup> 4p <sup>0.04</sup> 4d <sup>0.01</sup>	0.53
		Fe(2, 4)	[core]4s <sup>0.62</sup> 3d <sup>6.92</sup> 4p <sup>0.03</sup> 4d <sup>0.01</sup> 5p <sup>0.01</sup>	0.41
		P(5, 6)	[core]3s <sup>1.91</sup> 3p <sup>4.02</sup>	-0.94
	<b>C</b> <sub>2v</sub>	Fe(1,2)	[core]4s <sup>0.85</sup> 3d <sup>6.82</sup> 4p <sup>0.07</sup> 4d <sup>0.01</sup>	0.24
		P(3,4)	[core]3s <sup>1.91</sup> 3p <sup>3.88</sup>	-0.80
		Fe(5,6)	[core]4s <sup>0.60</sup> 3d <sup>6.78</sup> 4p <sup>0.05</sup> 4d <sup>0.02</sup>	0.55
Fe <sub>3</sub> P <sub>3</sub>	<b>C</b> <sub>3v</sub>	Fe(1, 2, 5)	[core]4s <sup>0.81</sup> 3d <sup>6.64</sup> 4p <sup>0.08</sup> 4d <sup>0.01</sup>	0.44
		P(3, 4, 6)	[core]3s <sup>1.90</sup> 3p <sup>3.54</sup>	-0.44

# Natural electron configurations and natural populations of Fe-P clusters (2)

System	Symm.	Atom	Natural electron configuration	Natural population
Fe <sub>3</sub> P <sub>3</sub>	<b>C</b> <sub>2v</sub>	Fe(1)	[core]4s <sup>0.54</sup> 3d <sup>6.85</sup> 4p <sup>0.05</sup> 4d <sup>0.01</sup>	0.55
		P(2, 4)	[core]3s <sup>1.91</sup> 3p <sup>3.80</sup>	-0.72
		P(3)	[core]3s <sup>1.93</sup> 3p <sup>3.48</sup>	-0.42
		Fe(5, 6)	[core]4s <sup>0.52</sup> 3d <sup>6.76</sup> 4p <sup>0.05</sup> 4d <sup>0.02</sup> 5p <sup>0.01</sup>	0.65
Fe <sub>2</sub> P <sub>4</sub>	D <sub>4h</sub>	P(1-4)	[core]3s <sup>1.91</sup> 3p <sup>3.36</sup>	-0.27
		Fe(5, 6)	[core]4s <sup>0.38</sup> 3d <sup>7.01</sup> 4p <sup>0.04</sup> 4d <sup>0.02</sup>	0.54
	<b>C</b> <sub>2v</sub>	Fe(1, 2)	[core]4s <sup>0.55</sup> 3d <sup>6.77</sup> 4p <sup>0.06</sup> 4d <sup>0.02</sup> 5p <sup>0.01</sup>	0.61
		P(3, 4)	[core]3s <sup>1.87</sup> 3p <sup>3.26</sup> 4p <sup>0.01</sup>	-0.14
		P(5,6)	[core]3s <sup>1.93</sup> 3p <sup>3.53</sup>	-0.47
FeP₅	<b>C</b> <sub>4v</sub>	P(1, 3)	[core]3s <sup>1.91</sup> 3p <sup>3.29</sup>	-0.21
		P(2, 4)	[core]3s <sup>1.91</sup> 3p <sup>3.22</sup>	-0.14
		Fe(5)	[core]4s <sup>0.41</sup> 3d <sup>6.88</sup> 4p <sup>0.05</sup> 4d <sup>0.01</sup>	0.64
		P(6)	[core]3s <sup>1.87</sup> 3p <sup>3.07</sup> 4p <sup>0.01</sup>	0.05
P <sub>6</sub>	D <sub>4h</sub>	P(1-4)	[core]3s <sup>1.93</sup> 3p <sup>3.09</sup>	-0.02

## Calculations on Fe<sub>6</sub> cluster

- Our calculated bond lengths are consistent with the previous results (2.29 - 2.53 Å) and are very close to nearest neighbour distance of bulk iron (2.48 Å), while calculated binding energy is smaller than the previous results (3.77 eV/ atom).
- The electron configuration calculated for Fe atom is 4s<sup>1.09</sup>3d<sup>6.80</sup> which is very close to that of the metal or large clusters (4s<sup>1</sup>3d<sup>7</sup>).



### Calculations on P<sub>6</sub> cluster

- For P<sub>6</sub> (D<sub>4h</sub>) cluster, our calculations find the M=3 ground state with bond length of 2.61 - 2.82 Å and binding energy of 1.09 eV/atom.
- The previous LSDA calculations based on the Car-Parrinello method on various structure of P<sub>6</sub> have predicted that bond length range from 2.01 to 2.40 Å. The binding energies of P<sub>6</sub> (C<sub>2v</sub> and D<sub>3h</sub>) clusters calculated using the generalized gradient approximations have predicted to be 3.06 and 3.02 eV/atom, respectively.
- The above differences between our calculations and previous calculations result from different treatment of electron in clusters rather than differences in structure and exchange-correlation energy. The spin-restricted calculations generally lead to shorter bond lengths and larger binding energies because of neglecting the spin dependence of exchange and correlation.



## Effects of P substitutions (I)

#### Effects on binding energy:

- $\bigcirc$  Fe<sub>3</sub>P<sub>3</sub> and Fe-rich clusters have larger binding energies.
- O P-rich clusters have smaller binding energies.

#### Effects on bonding strength:

- In the Fe<sub>3</sub>P<sub>3</sub> (C<sub>2v</sub>) and Fe-rich clusters, the stronger Fe-P and weaker Fe-Fe bondings caused by the charge transfer due to the P substitutions.
- O In Fe<sub>3</sub>P<sub>3</sub> (C<sub>3v</sub>) cluster, stabilization of Fe3 and P3 units lead to the weaker Fe-P bonding.
- In P-rich clusters, decrease in binding energies corresponds to the weaker Fe-P and P-P bondings.



## Effects of P substitutions (2)

Effects on electronic structure:

The P substitution causes the charge transfer from Fe to P atoms.
The charge transfer leads to the stronger and weaker bondings in Fe-P clusters.

The P embrittlement of Fe GB is closely connected with the change of electronic structure due to atomic configurations of P atoms in GBs.



### Thank you for your stop.

If you have a interest in this work, please contact me.

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